

# Scale hierarchies and string cosmology

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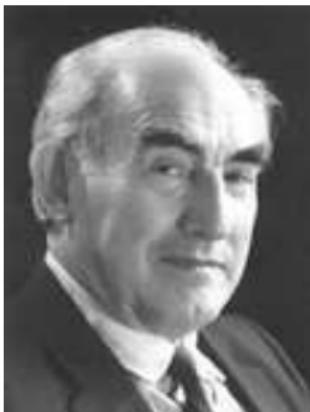
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and

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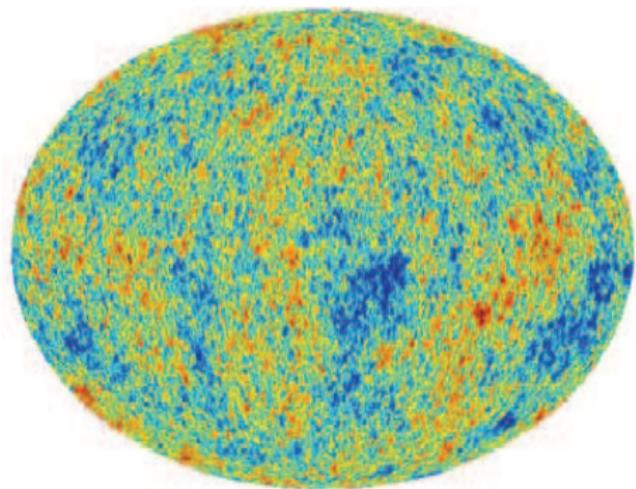
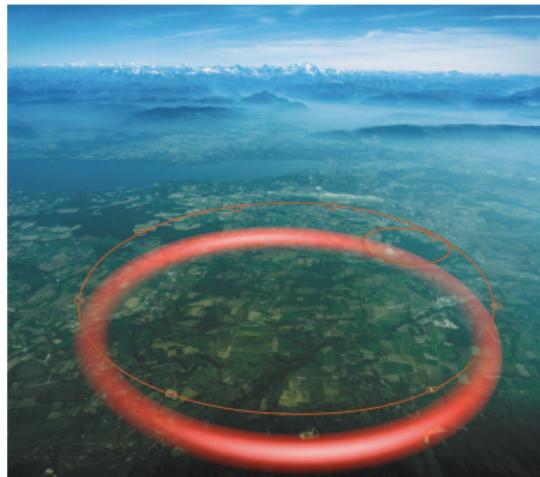
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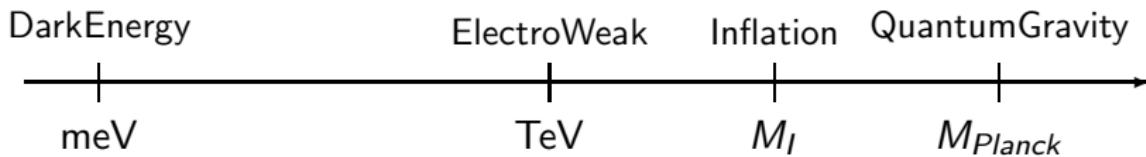
# String theory

- Is it a tool for strong coupling dynamics or a theory of fundamental forces?
- If theory of Nature can it describe both particle physics and cosmology?

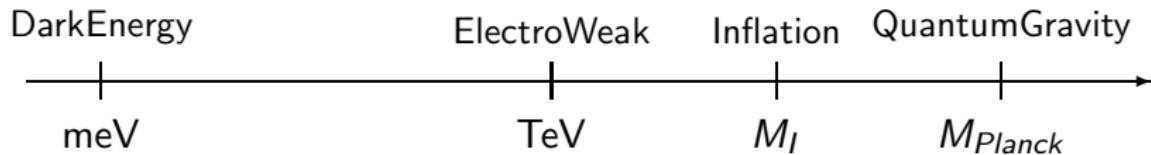


# Problem of scales

- describe high energy (**SUSY?**) extension of the Standard Model  
unification of all fundamental interactions
  - incorporate Dark Energy  
simplest case: infinitesimal (tunable) +ve cosmological constant
  - describe possible accelerated expanding phase of our universe  
models of inflation (approximate de Sitter)
- ⇒ 3 very different scales besides  $M_{Planck}$  :



# Problem of scales



- ① they are independent
- ② possible connections
  - $M_I$  could be near the EW scale, such as in Higgs inflation  
but large non minimal coupling to explain
  - $M_{Planck}$  could be emergent from the EW scale  
in models of low-scale gravity and TeV strings

What about  $M_I$ ? can it be at the TeV scale?

Can we infer  $M_I$  from cosmological data?

I.A.-Patil '14 and '15

- connect inflation and SUSY breaking scales

# impose independent scales: proceed in 2 steps

- ① SUSY breaking at  $m_{SUSY} \sim \text{TeV}$

with an infinitesimal (tunable) positive cosmological constant

Villadoro-Zwirner '05

I.A.-Knoops, I.A.-Ghilencea-Knoops '14, I.A.-Knoops '15

- ② Inflation connected or independent? [21]

# Toy model for SUSY breaking

Content (besides  $N = 1$  SUGRA): one vector  $V$  and one chiral multiplet  $S$   
with a shift symmetry  $S \rightarrow S - ic\omega \leftarrow$  transformation parameter

String theory: compactification modulus or universal dilaton

$$s = 1/g^2 + ia \leftarrow \text{dual to antisymmetric tensor}$$

Kähler potential  $K$ : function of  $S + \bar{S}$

$$\text{string theory: } K = -\rho \ln(S + \bar{S})$$

Superpotential: constant or single exponential if R-symmetry  $W = ae^{bS}$

$$\int d^2\theta W \text{ invariant}$$

$$b < 0 \Rightarrow \text{non perturbative}$$

can also be described by a generalized linear multiplet [17]

# Scalar potential

$$\mathcal{V}_F = a^2 e^{\frac{b}{l}} l^{p-2} \left\{ \frac{1}{p} (pl - b)^2 - 3l^2 \right\} \quad l = 1/(s + \bar{s})$$

Planck units

- $b > 0 \Rightarrow$  SUSY local minimum in AdS space with  $l = b/p$
- $b \leq 0 \Rightarrow$  no minimum with  $l > 0$  ( $p \leq 3$ )  
but interesting metastable SUSY breaking vacuum

when R-symmetry is gauged by  $V$  allowing a Fayet-Iliopoulos (FI) term:

$$\mathcal{V}_D = c^2 l (pl - b)^2 \quad \text{for gauge kinetic function } f(S) = S$$

- $b > 0$ :  $\mathcal{V} = \mathcal{V}_F + \mathcal{V}_D$  SUSY AdS minimum remains
- $b = 0$ : SUSY breaking minimum in AdS ( $p < 3$ ) [15]
- $b < 0$ : SUSY breaking minimum with tuneable cosmological constant  $\Lambda$

## Scalar potential for $b = 0$

$$V = a^2(p - 3)l^p + c^2p^2l^3$$

can be obtained for  $p = 2$  and  $l$  the string dilaton:

- all geometric moduli fixed by fluxes in a SUSY way
- D-term contribution : D-brane potential (uncancelled tension)
- F-term contribution : tree-level potential (away from criticality)

String realisation : framework of magnetised branes

# Type I string theory with magnetic fluxes $B_{ij}$ on 2-cycles of the compactification manifold

- Dirac quantization:  $B = \frac{m}{nA} \equiv \frac{p}{A}$  [12]  $\Rightarrow$  moduli stabilization  
 $B$ : constant magnetic field       $m$ : units of magnetic flux  
 $n$ : brane wrapping       $A$ : area of the 2-cycle
- Spin-dependent mass shifts for charged states  $\Rightarrow$  SUSY breaking
- Exact open string description:  $\Rightarrow$  calculability  
 $qB \rightarrow \theta = \arctan qB\alpha'$  weak field  $\Rightarrow$  field theory
- T-dual representation: branes at angles  $\Rightarrow$  model building  
( $m, n$ ): wrapping numbers around the 2-cycle directions

explicit examples: e.g.  $T^6$  toroidal compactification

I.A.-Maillard '04, I.A.-Kumar-Maillard '05, '06, Bianchi-Trevigne '05

- all geometric moduli can be stabilized in a supersymmetric way  
need 9 magnetized  $U(1)$ s (branes)
- however tadpole (anomaly) cancellation requires an extra  $U(1)$  brane  
 $\Rightarrow$  dilaton potential [13] I.A.-Derendinger-Maillard '08

its form is fixed by the axion shift symmetry

$\Rightarrow$  break SUSY with tuneable vacuum energy

I.A.-Knoops '14, '15

# Magnetic fluxes can be used to stabilize moduli

I.A.-Maillard '04, I.A.-Kumar-Maillard '05, '06, Bianchi-Trevigne '05

e.g.  $T^6$ : 36 moduli (geometric deformations)

internal metric:  $6 \times 7/2 = 21 = 9 + 2 \times 6$

type IIB RR 2-form:  $6 \times 5/2 = 15 = 9 + 2 \times 3$

complexification  $\Rightarrow \begin{cases} \text{K\"ahler class} & J \\ \text{complex structure} & \tau \end{cases}$  9 complex moduli for each

magnetic flux:  $6 \times 6$  antisymmetric matrix  $F$  complexification  $\Rightarrow$

$F_{(2,0)}$  on holomorphic 2-cycles: potential for  $\tau$  superpotential

$F_{(1,1)}$  on mixed (1,1)-cycles: potential for  $J$  FI D-terms

# $N=1$ SUSY conditions $\Rightarrow$ moduli stabilization

- ①  $F_{(2,0)} = 0 \Rightarrow \tau$  matrix equation for every magnetized  $U(1)$

$$\tau^T p_{xx} \tau - (\tau^T p_{xy} + p_{yx} \tau) + p_{yy} = 0 \quad [9]$$

$T^6$  parametrization:  $(x^i, y^i) \quad i = 1, 2, 3 \quad z^i = x^i + \tau^{ij} y^j$

need 'oblique' (non-commuting) magnetic fields to fix off-diagonal components of the metric  $\leftarrow$  but can be made diagonal

- ②  $J \wedge J \wedge F_{(1,1)} = F_{(1,1)} \wedge F_{(1,1)} \wedge F_{(1,1)} \Rightarrow J$

vanishing of a Fayet-Iliopoulos term:  $\xi \sim F \wedge F \wedge F - J \wedge J \wedge F$

magnetized  $U(1) \rightarrow$  massive absorbs RR axion

one condition  $\Rightarrow$  need at least 9 brane stacks

- ③ Tadpole cancellation conditions : introduce an extra brane(s) [10]

$N = 2$  non-linear supersymmetry  $\Rightarrow$

General form of the localized dilaton potential:

$$V(\phi, d) = \frac{e^{-\phi}}{g^2} \left\{ \left( \sqrt{1 - d^2} - 1 \right) + \xi d + \delta T \right\}$$

↗ DBI action      ↗ FI-term

$d$ : D-auxiliary in  $2\pi\alpha'$ -units

$\delta T$ : tension leftover RR tadpole cancellation  $\Rightarrow \delta T = 1 - \sqrt{1 - \xi^2}$

$$d \text{ elimination} \Rightarrow d = \frac{\xi}{\sqrt{1+\xi^2}}$$

$$V_{\min} = \delta \bar{T} e^{-\phi} ; \quad \delta \bar{T} = \sqrt{1 + \xi^2} - \sqrt{1 - \xi^2}$$

# Dilaton fixing

add a ‘non-critical’ dilaton potential

⇒ AdS vacuum with tuneable string coupling

$$V_{\text{non-crit}} = \delta c e^{-2\phi} \quad \delta c: \text{central charge deficit}$$

minimization of  $V = V_{\text{non-crit}} + V_D \Rightarrow \delta c < 0$

$$e^{\phi_0} = -\frac{2\delta c}{3\delta T} \quad V_0 = \frac{\delta c^3}{3\delta T^2} \quad R_0 = -\delta T e^{3\phi_0}$$

$\nwarrow$  curvature in Einstein frame

e.g. replace a free coordinate by a CFT minimal model of central charge  $1 + \delta c$

→ generalize: add a dilaton potential preserving the axion shift symmetry

⇒ break SUSY with tuneable vacuum energy [8]

I.A.-Knoops '14, '15

# minimisation and spectrum

Minimisation of the potential:  $V' = 0, V = \Lambda$

In the limit  $\Lambda \approx 0$  ( $p = 2$ )  $\Rightarrow$  [7] [23]

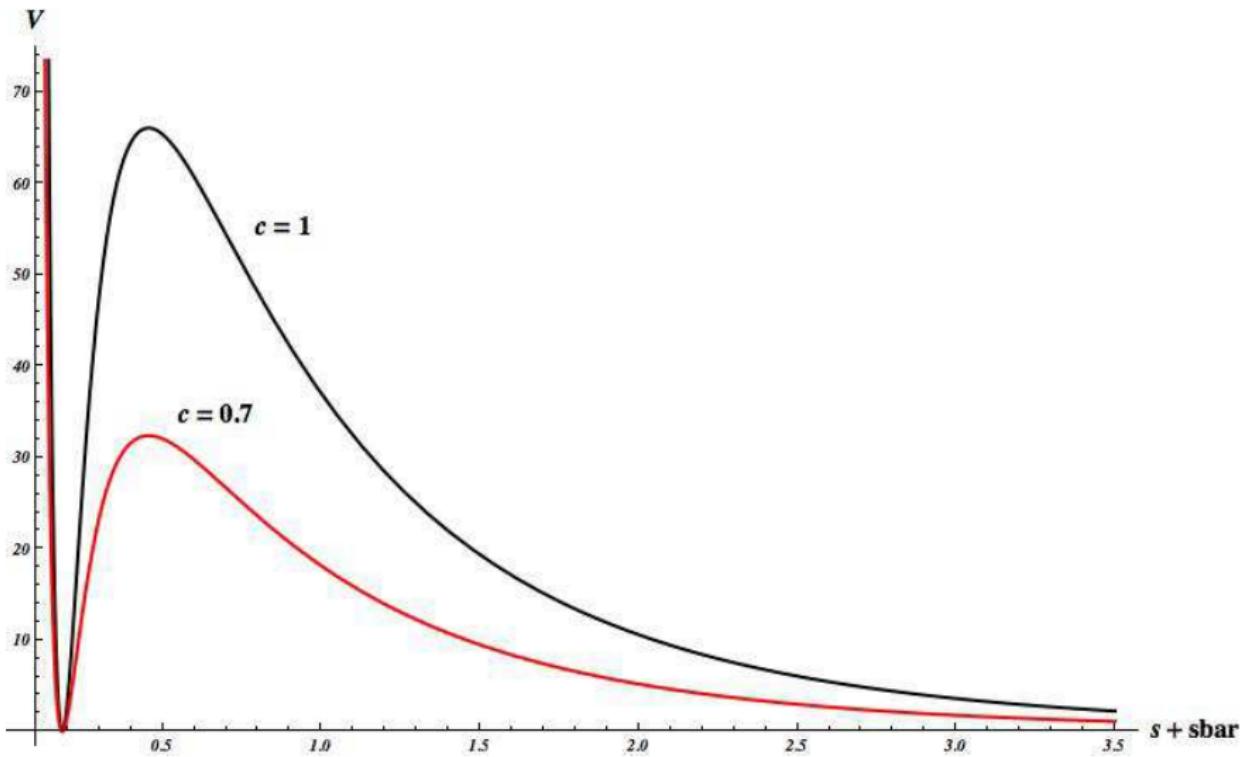
$$b/l = \rho \approx -0.183268 \quad \Rightarrow \langle l \rangle = b/\rho$$

$$\frac{a^2}{bc^2} = 2\frac{e^{-\rho}}{\rho} \frac{(2-\rho)^2}{2+4\rho-\rho^2} + \mathcal{O}(\Lambda) \approx -50.6602 \quad \Rightarrow c \propto a$$

Physical spectrum:

massive dilaton,  $U(1)$  gauge field, Majorana fermion, gravitino

All masses of order  $m_{3/2} \approx e^{\rho/2}/a \leftarrow$  TeV scale



[21]

# Properties and generalizations

- Metastability of the ground state: extremely long lived

$$I \simeq 0.02 \text{ (GUT value } \alpha_{GUT}/2) \text{ } m_{3/2} \sim \mathcal{O}(TeV) \Rightarrow$$

decay rate  $\Gamma \sim e^{-B}$  with  $B \approx 10^{300}$

- Add visible sector (MSSM) preserving the same vacuum matter fields  $\phi$  neutral under R-symmetry

$$K = -2 \ln(S + \bar{S}) + \phi^\dagger \phi \quad ; \quad W = (a + W_{MSSM}) e^{bS}$$

$\Rightarrow$  soft scalar masses non-tachyonic of order  $m_{3/2}$  (gravity mediation)

- Toy model classically equivalent to [6]

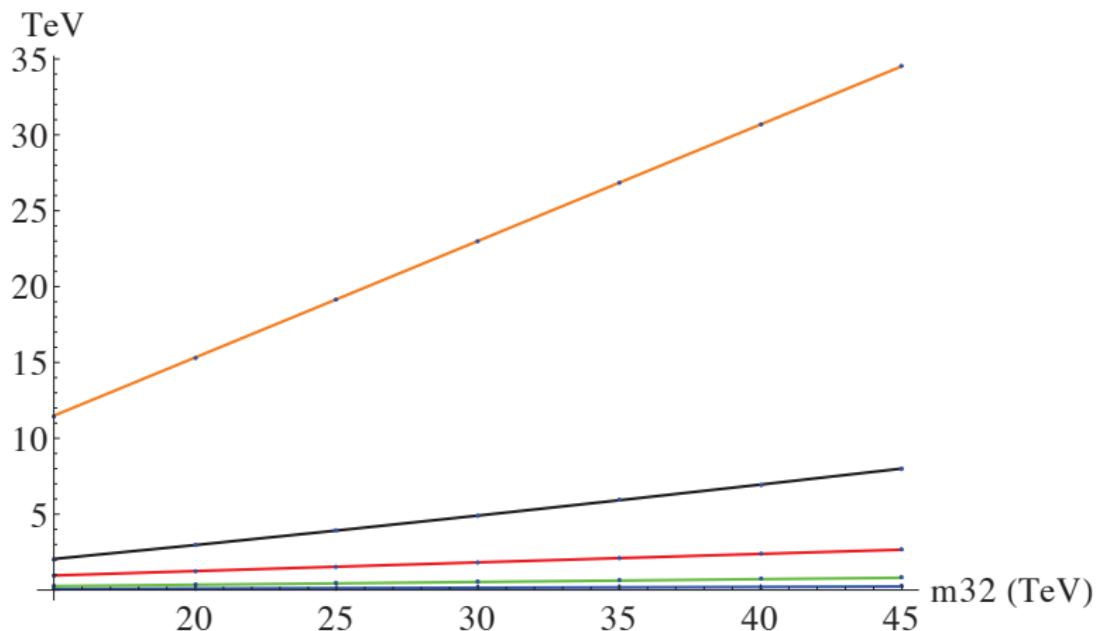
$$K = -p \ln(S + \bar{S}) + b(S + \bar{S}) \quad ; \quad W = a \quad \text{with } V \text{ ordinary } U(1)$$

- Dilaton shift can be identified with  $B - L \supset \text{matter parity } (-)^{B-L}$

# Properties and generalizations

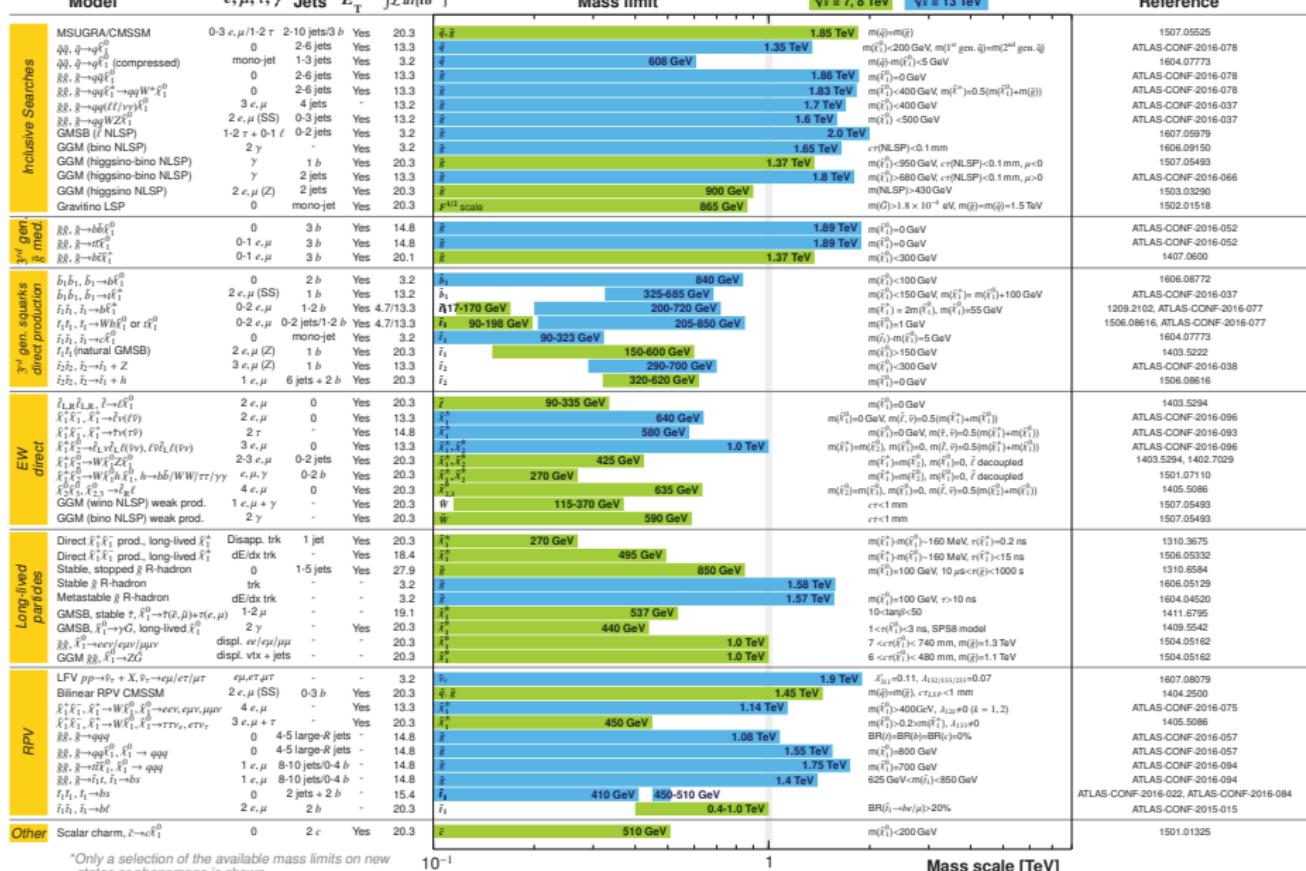
- R-charged fields needed for anomaly cancellation
- A simple (anomaly free) variation:  $f = 1$  and  $p = 1$   
tuning still possible but scalar masses of neutral matter tachyonic  
possible solution: add a new field  $Z$  in the 'hidden' SUSY sector  
 $\Rightarrow$  one extra parameter
- alternatively: add an  $S$ -dependent factor in Matter kinetic terms  
$$K = -\ln(S + \bar{S}) + (S + \bar{S})^{-\nu} \sum \Phi \bar{\Phi} \quad \text{for } \nu \gtrsim 2.5$$
  
or the  $B - L$  unit charge of SM particles  $\Rightarrow$  similar phenomenology
- distinct features from other models of SUSY breaking and mediation
- gaugino masses at the quantum level  
 $\Rightarrow$  suppressed compared to scalar masses and A-terms

# Typical spectrum



The masses of sbottom squark (yellow), stop (black), gluino (red), lightest chargino (green) and lightest neutralino (blue) as a function of the gravitino mass. The mass of the lightest neutralino varies between  $\sim 40$  and  $150$  GeV [5]

Status: August 2016



\*Only a selection of the available mass limits on new states or phenomena is shown.

# Inflation from the SUSY breaking sector

I.A.-Chatrabhuti-Isono-Knoops '16

Can the dilaton be the inflaton in the simple model of SUSY breaking based on a gauged shift symmetry?

the only physical scalar left over, partner (partly) of the goldstino

partly because of a D-term auxiliary component

Same potential cannot satisfy the slow roll condition  $|\eta| = |V''/V| \ll 1$

with the dilaton rolling towards the Standard Model minimum

⇒ need to create an appropriate plateau around the maximum of  $V$  [16]

without destroying the properties of the SM minimum

⇒ study possible corrections to the Kähler potential

only possibility compatible with the gauged shift symmetry

# Extensions of the SUSY breaking model

Parametrize the general **correction** to the Kähler potential:

$$K = -p\kappa^{-2} \log \left( s + \bar{s} + \frac{\xi}{b} F(s + \bar{s}) \right) + \kappa^{-2} b(s + \bar{s})$$

$$W = \kappa^{-3} a, \quad f(s) = \gamma + \beta s$$

$$\mathcal{P} = \kappa^{-2} c \left( b - p \frac{1 + \frac{\xi}{b} F'}{s + \bar{s} + \frac{\xi}{b} F} \right)$$

Three types of possible corrections:

- perturbative:  $F \sim (s + \bar{s})^{-n}$ ,  $n \geq 0$
- non-perturbative D-brane instantons:  $F \sim e^{-\delta(s+\bar{s})}$ ,  $\delta > 0$
- non-perturbative NS5-brane instantons:  $F \sim e^{-\delta(s+\bar{s})^2}$ ,  $\delta > 0$

Only the last can lead to slow-roll conditions with sufficient inflation

# Slow-roll inflation

$F = \xi e^{\alpha b^2 \phi^2}$  with  $\phi = s + \bar{s} = 1/l \Rightarrow$  two extra parameters  $\alpha < 0, \xi$   
they control the shape of the potential

slow-roll conditions:  $\epsilon = 1/2(V'/V)^2 \ll 1, |\eta| = |V''/V| \ll 1$   
 $\Rightarrow$  allowed regions of the parameter space with  $|\xi|$  small

additional independant parameters:  $a, c, b$

SM minimum with tuneable cosmological constant  $\Lambda$ :  $V' = 0, V = \Lambda \approx 0$

$\xi = 0 \Rightarrow b\phi_{min} = \rho_0, \frac{a^2}{bc^2} = \lambda_0$  with  $\rho_0, \lambda_0$  calculable constants [15]

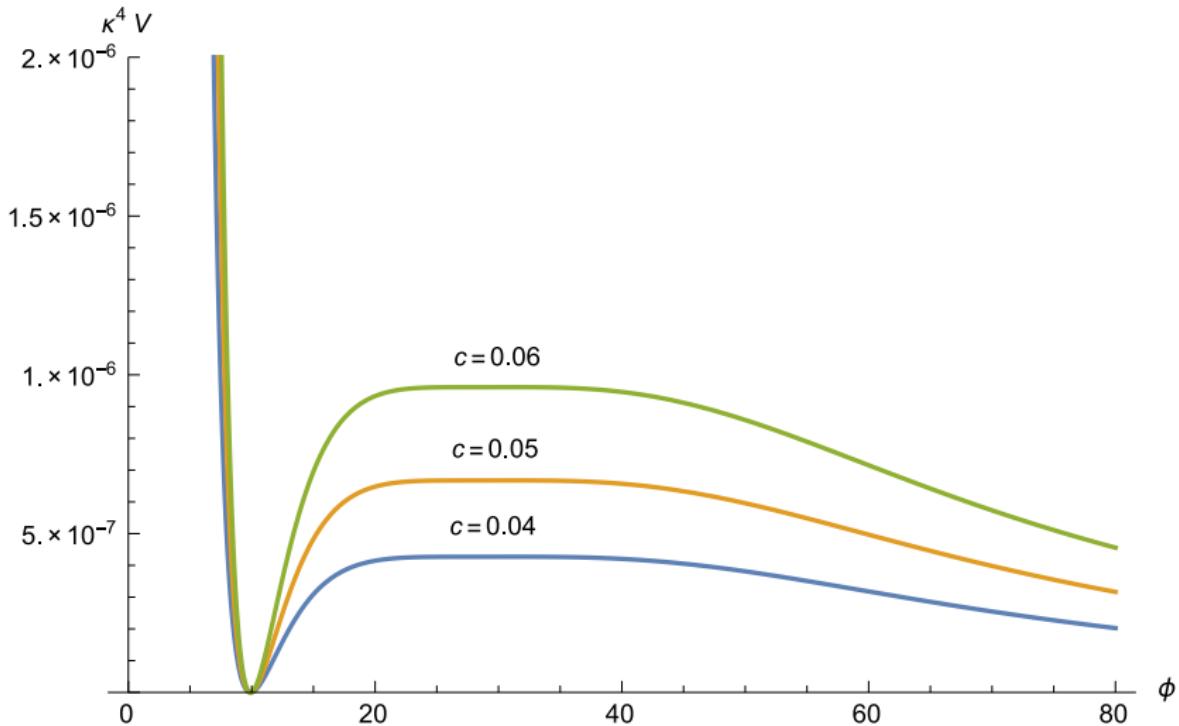
$b$  controls  $\phi_{min} \sim 1/g_s$  choose it of order 10

tuning determines  $a$  in terms of  $c$  overall scale of the potential

$\xi \neq 0 \Rightarrow \rho_0, \lambda_0$  become functions  $I(\xi, \alpha), \lambda(\xi, \alpha)$

numerical analysis  $\Rightarrow$  mild dependence

$$\xi = 0.025, \alpha = -4.8, p = 2, b = -0.018$$



# Fit Planck '15 data and predictions

inflation starts with an initial condition for  $\phi = \phi_*$  near the maximum and ends when  $|\eta| = 1$

$$\Rightarrow \text{number of e-folds } N = \int_{\text{end}}^{\text{start}} \frac{V}{V'}$$

Predictions for the power spectrum of perturbations in CMB:

amplitude of density perturbations  $A_s = \frac{\kappa^4 V_*}{24\pi^2 \epsilon_*}$

spectral index  $n_s = 1 + 2\eta_* - 6\epsilon_*$

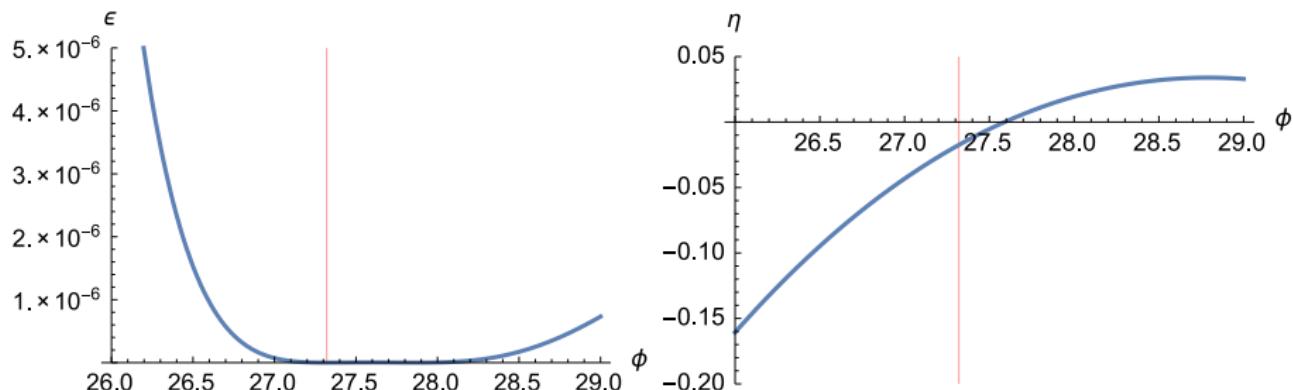
tensor – to – scalar ratio  $r = 16\epsilon_*$

Numerical analysis: fit Planck '15 data and keep the SM minimum with an infinitesimal cosmological constant

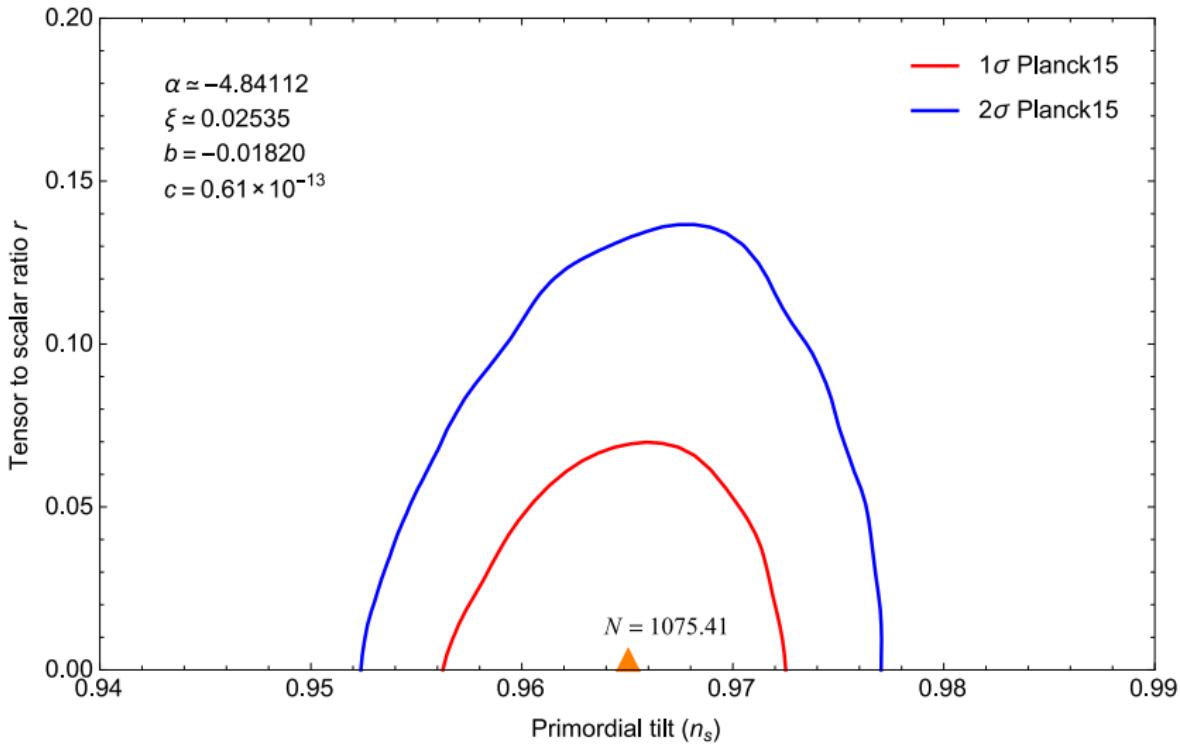
$\Rightarrow$  fine tuning of the parameters of the model

# Fit Planck '15 data and predictions

$$p = 2, \phi_* = 27.32, \xi = 0.025, \alpha = -4.8, b = -0.018, c = 0.61 \times 10^{-13}$$



$N$	$n_s$	$r$	$A_s$
1075	0.965	$3 \times 10^{-23}$	$2.259 \times 10^{-9}$



$p = 1$ : similar analysis  $\Rightarrow$

$$\phi_* = 64.53, \xi = 0.30, \alpha = -0.78, b = -0.023, c = 10^{-13}$$

N	$n_s$	r	$A_s$
889	0.959	$4 \times 10^{-22}$	$2.205 \times 10^{-9}$

SM minimum:  $\langle \phi \rangle \approx 21.53, \langle m_{3/2} \rangle = 18.36 \text{ TeV}, \langle M_{A_\mu} \rangle = 36.18 \text{ TeV}$

During inflation:

$$H_* = \kappa \sqrt{\mathcal{V}_*/3} = 5.09 \text{ TeV}, \quad m_{3/2}^* = 4.72 \text{ TeV}, \quad M_{A_\mu}^* = 6.78 \text{ TeV}$$

Low energy spectrum essentially the same with  $\xi = 0$ :

$$m_0^2 = m_{3/2}^2 [-2 + \mathcal{C}], \quad A_0 = m_{3/2} \mathcal{C}, \quad B_0 = A_0 - m_{3/2}$$

$\mathcal{C} = 1.53$  vs at  $\xi = 0$ :  $\mathcal{C}_0 = 1.52, m_{3/2}^0 = 17.27$ , although  $\langle \phi \rangle_0 \approx 9.96$

# Conclusions

String phenomenology:

Consistent framework for particle physics and cosmology

**Challenge of scales:** at least three very different (besides  $M_{Planck}$ )  
electroweak, dark energy, inflation, SUSY?

their origins may be connected or independent

SUSY with infinitesimal (tuneable) +ve cosmological constant

- interesting framework for model building incorporating dark energy
- identify inflaton with goldstino superpartner  
inflation at the SUSY breaking scale (TeV?)